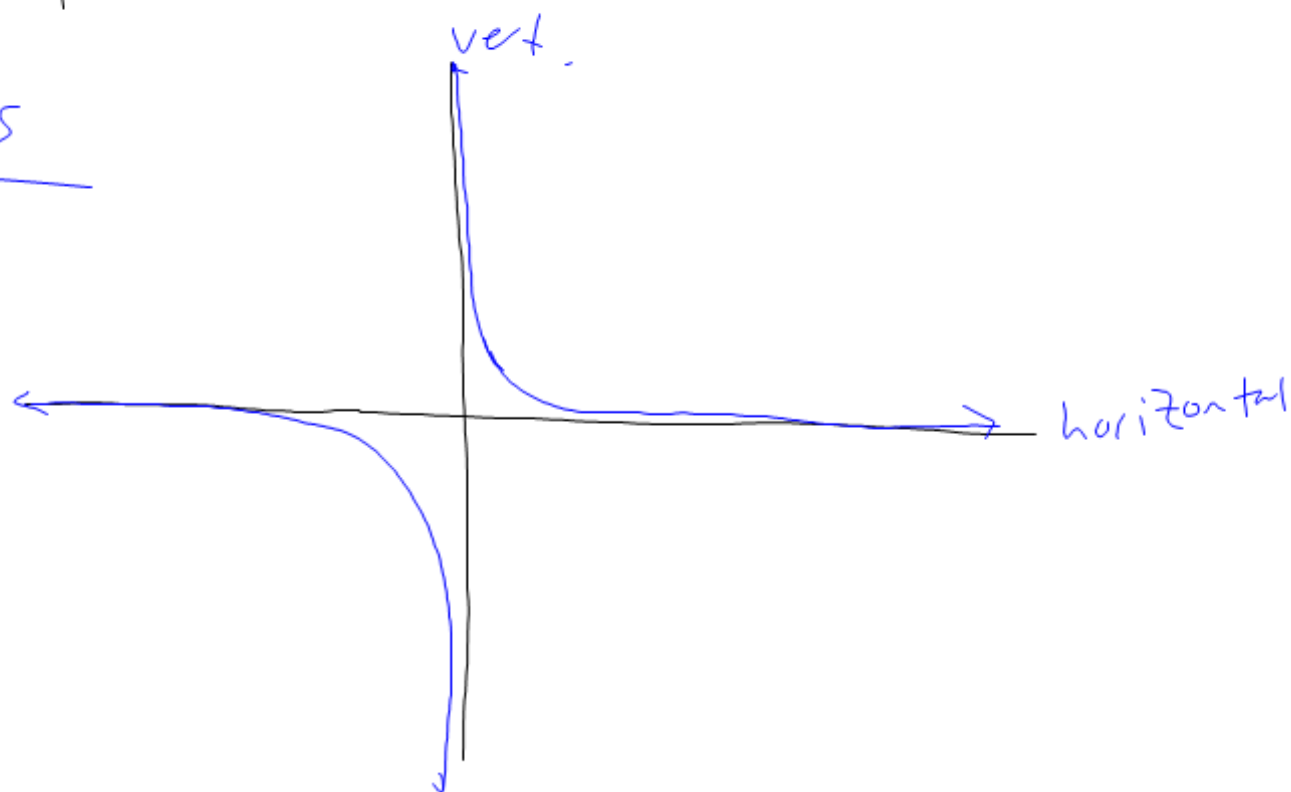


$$f(x) = \frac{1}{x}$$

x	-1000	-100	-1	0	1	100	1000	0.1	0.01
f(x)	-0.001	-0.01	-1	undef.	1	0.01	0.001	10	100

asymptotes



$$f(x) = \frac{N(x)}{D(x)} = \frac{\text{some polynomial}}{\text{some polynomial}} \cdot \text{ex } \frac{3x^3 + 5x^2 + 6}{2x^2 + 7x - 8}$$

① Vert. asymptotes happens at zeros of $D(x)$

② Horizontal Asymptotes (n is power of top, m is power bottom)

(a) If $n > m$, no horizontal asymptote

$$\frac{x^2 + 4}{3x - 1}, \text{ grow out bound}^*$$

(b) If $m > n$, $y = 0$ is the horz. asymptote

$$\frac{3x - 1}{x^2 + 4}, \text{ as } x \text{ grows, } D(x) \text{ gets much larger, overall approaches zero}$$

(c) If $m = n$, horz asymptote at $y = \frac{\text{leading coefficient}}{\text{leading coefficient}}$

$$\frac{3x^2 - 1}{x^2 + 4}, \text{ has asymptote at } y = \frac{3}{1}$$

Find all asymptotes - No Calc.

(a) $f(x) = \frac{2x}{3x^2+1}$

, horz. asymptotes

powers
bottom top
 $m > n$,

so $y=0$ is
horz. asymptotes

$$3x^2+1=0$$

$$-1 \quad -1$$

$$3x^2 = -1$$

$$\sqrt{x^2} = \sqrt{-\frac{1}{3}}$$

non real All \mathbb{R}

No vert.
asymptotes

(b) $f(x) = \frac{2x^2}{x^2-1}$

horz = $\frac{2}{1}$

All $\mathbb{R} x \neq \pm 1$
vert = ± 1

$$x^2-1=0 \quad \sqrt{x^2}=\sqrt{1} \quad x=\pm 1$$

(c) $f(x) = \frac{x^2+x-2}{x^2-x-6}$

horz = $\frac{1}{1}$

vert = 3, ~~-2~~
All \mathbb{R}
 $x \neq -2, 3$

$$\frac{(x+2)(x-1)}{(x+2)(x-3)}$$

(d) $f(x) = \frac{3x^3+7x^2+2}{-4x^3+5}$

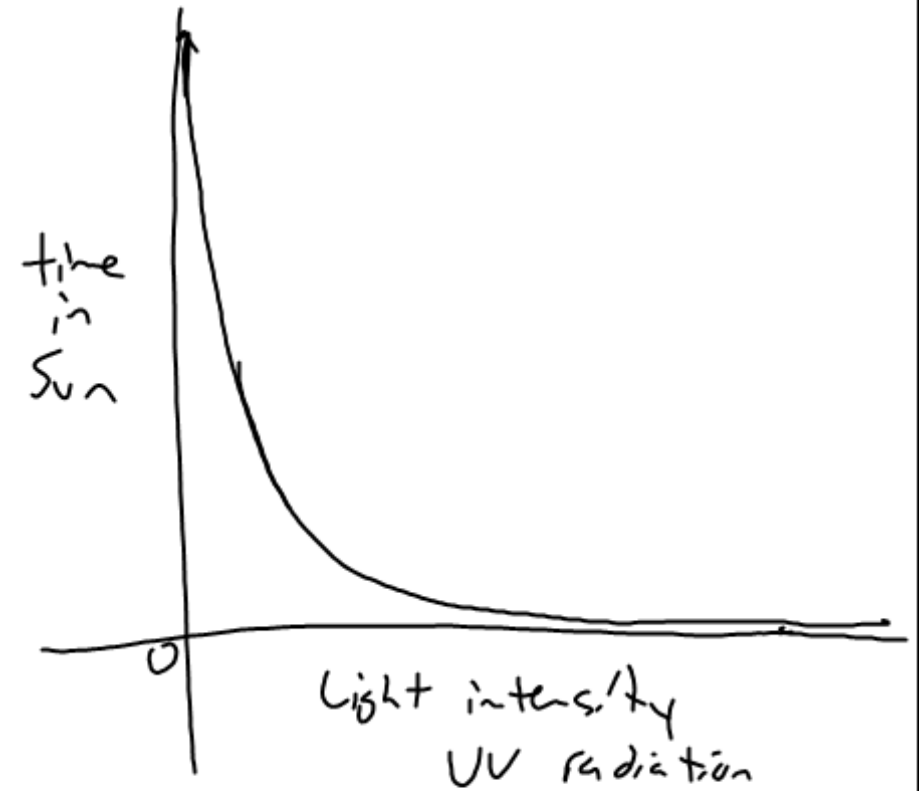
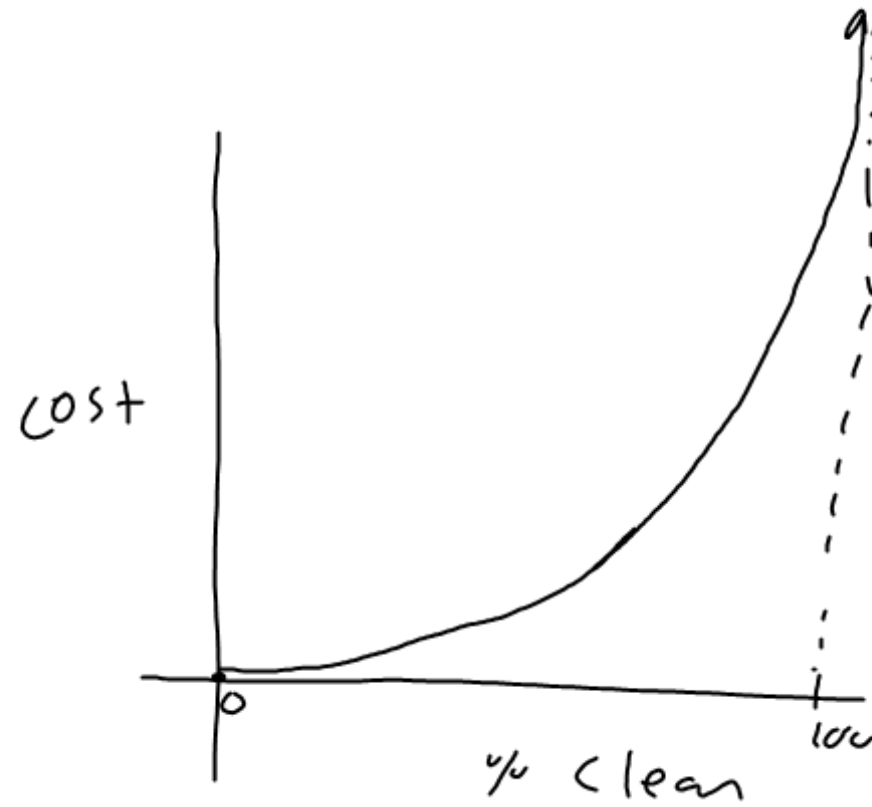
horz = $-\frac{3}{4}$, vert

$$-4x^3+5=0$$

$$x = \sqrt[3]{\frac{5}{4}}$$

All \mathbb{R}
 $x \neq \sqrt[3]{\frac{5}{4}}$

$$f(x) = \frac{x-1}{x-3}$$



Sect. 2.6

#1-6 b + c ,

7-12 matching
NO
CALC

[HW]

#13-21 (odd), 23, 27, 28, 31-34

zeros of $f(x)$ are the zeros of the top, unless one is
an asymptote